مسابقة في مادة الفيزياء المدة ثلاث ساعات

This exam is formed of four exercises in four pages numbered from 1 to 4.The use of non-programmable calculator is recommended.

### First exercise: (7.5 points)

### Horizontal mechanical oscillator

A horizontal mechanical oscillator is formed of a puck (S), of mass m = 510 g, attached to two identical

springs of un-jointed loops whose other extremities

A and B are connected to two fixed supports. Each spring is of negligible mass, natural length  $\ell_0$  and stiffness k = 10 Nm<sup>-1</sup>. (S) may slide along a horizontal air table and its center of inertia G can then move along a horizontal axis x'Ox.

الأسم: الرقم:

At equilibrium (Fig. 1):

- G coincides with the origin O of the axis x'x;
- each spring is elongated by  $\Delta \ell$  such that its length is  $\ell = \ell_0 + \Delta \ell$ .

The horizontal plane passing through G is taken as a reference level of gravitational potential energy. **A** – **Theoretical Study** 

(S) is supposed to oscillate without friction. At an instant t, the abscissa of G is  $x = \overline{OG}$ , the algebraic

value of its velocity is  $v = \frac{dx}{dt}$  and the two springs have lengths  $\ell_1$  and  $\ell_2$  (Fig. 2).

- a) Referring to figure 2, express l<sub>1</sub> and l<sub>2</sub> in terms of l and x.
   b) Show that, at an instant t, the total elastic potential energy stored in the two springs is given by: PE<sub>e</sub> = k[(Δl)<sup>2</sup> + x<sup>2</sup>].
- 2) Write down, at an instant t, the expression of the mechanical energy of the system (puck, two springs, Earth) in terms of v, m, k,  $\Delta \ell$  and x.
- **3)** Derive the second order differential equation in x that describes the motion of G.
- 4) The solution of the differential equation is of the form:  $x = X_m \cos(\omega_0 t + \phi)$  where  $X_m$ ,  $\omega_0$  and  $\phi$  are constants.
  - a) Determine, in terms of k and m, the expression of ω<sub>0</sub>.
    b) Deduce the value T<sub>0</sub> of the proper period of the oscillations of G.

## **B** – Experimental study

An appropriate apparatus allows the recording of the abscissa x of G as a function of time (Fig. 3)

- a) The experimental value of the period T is slightly different from the theoretical value T<sub>0</sub>. Indicate the cause of this difference.
  - **b**) Determine, referring to figure 3, the period T of the oscillations of G.
- 2) At t = 4.04 s, the amplitude of the oscillations is 2.36 cm.
  - a) Determine the mechanical energy lost by the system (puck, two springs, Earth) between the instants  $t_0 = 0$  and t = 4.04 s.

-3

**b**) Deduce the average power lost in this interval.

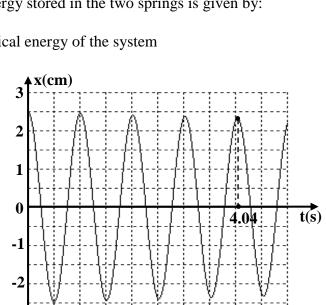
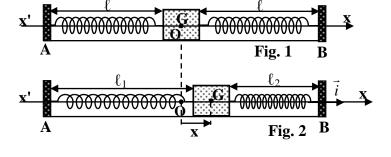


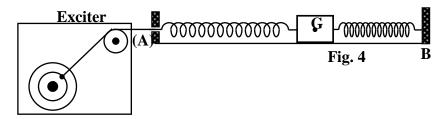
Fig. 3



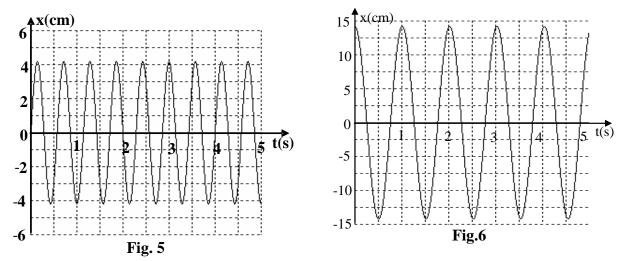
3) The extremity A of the left spring is coupled to an exciter (E) of adjustable frequency « f » (Fig. 4). With an appreciable amount of friction, the puck is forced to oscillate on the air table with a frequency

equal to that of (E). The variations, as a function of time, of the abscissa x of G is represented for two values of  $\ll$  f » by figures 5 and 6.

**a**) Determine, in each case, the amplitude and the period of the oscillations of G.



**b**)The amplitude of the oscillations represented in figure 6 is larger than that of the oscillations of figure 5. Interpret this increase.



#### <u>Second exercise</u>: (7.5 points) Determination of the characteristics of a coil

In order to determine the characteristics of a coil, we consider the electric circuit represented in figure1. This circuit is formed of a capacitor of capacitance C, the coil of inductance L and of resistance r, a resistor of resistance R and an ammeter (A) of negligible resistance, all connected in series across an LFG, of adjustable frequency f, that maintains across its terminals an alternating sinusoidal voltage :

$$\mathbf{u} = \mathbf{u}_{AM} = \mathbf{U}\sqrt{2}\,\sin(2\pi\mathbf{ft} + \mathbf{\phi}).$$

Thus the circuit carries an alternating sinusoidal current:  $i = I\sqrt{2} \sin(2\pi ft)$  (Fig.1). A – 1) Write the expression of the voltage:

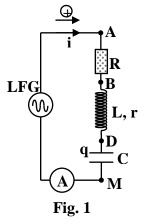
- **a**)  $u_{AB}$  across the terminals of the resistor in terms of R, I, f and t;
- **b**)  $u_{BD}$  across the terminals of the coil in terms of r, L, I, f and t.

2) Show that the voltage across the terminals of the capacitor is:

$$u_{\rm DM} = - \frac{I\sqrt{2}}{2\pi f C} \cos(2\pi f t).$$

B-1) Applying the law of addition of voltages and giving t two particular values, show that:

- **a**) The effective value of the current is: I =  $\frac{U}{\sqrt{(R+r)^2 + (2\pi f L \frac{1}{2\pi f C})^2}};$
- **b**) The phase difference  $\varphi$  between the voltage  $u_{AM}$  and the current i is:  $\tan \varphi = \frac{2\pi f L \frac{1}{2\pi f C}}{R + r}$

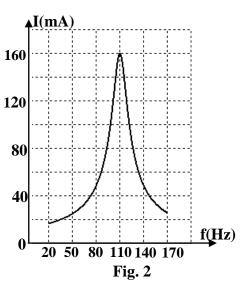


2) U is maintained constant and f is varied; the ammeter indicates a value I for each value of f. An appropriate device allows to plot the curve representing the variation of I as a function of f (Fig. 2).

This curve shows an evidence of a physical phenomenon

for  $f = f_0 = 110$  Hz.

- a) Name this phenomenon.
- **b**) Indicate the value  $I_0$  of I corresponding to the value  $f_0$  of f.
- c) For  $f = f_0$ , show that:
  - i)  $4\pi^2 f_0^2 LC = 1$  using the relation given in part (B-1-b);
  - ii) the circuit is equivalent to a resistor of resistance  $R_t = R + r$ using the relation given in part (B-1-a).
- **d**) Calculate the value of L knowing that  $C = 21\mu F$ .
- e) Calculate the resistance r knowing that U = 8 V and  $R = 30 \Omega$ .



#### Third exercise: (7.5 points)

#### Nuclear submarine

A nuclear submarine is powered with a nuclear reactor using uranium 235. We intend to determine the efficiency of the reactor of this submarine that consumes 112 g of uranium 235 per day.

Take:  $c = 3 \times 10^8$  m/s; 1 MeV =  $1.6 \times 10^{-13}$  J; mass of 1 atom of uranium  $235 = 3.9 \times 10^{-25}$  kg.

1) One of the nuclear reactions that take place inside the reactor is:

$${}^{1}_{0}n + {}^{235}_{92}U \longrightarrow {}^{91}_{36}\mathrm{Kr} + {}^{\mathrm{Y}}_{\mathrm{X}}\mathrm{Ba} + {}^{1}_{0}n$$

- **a**) Determine the values of X and Y.
- **b**) Is the previous reaction provoked or spontaneous? Justify.
- c) Give the condition satisfied by the projectile neutron for this reaction to take place.
- 2) The adjacent table gives the binding energy per nucleon
  - $\frac{E_{B}}{E_{B}}$  of the involved nuclei.

А

- **a**) Calculate the binding energy  $E_B$  of each nucleus.
- **b**) Write the expression of the binding energy  $E_B$  of a nucleus  $_{Z}^{A}X$  in terms of A, Z,  $m_{x}$  [mass of the nucleus],  $m_{P}$  [mass of a proton] and  $m_{n}$  [mass of a neutron].
- c) Show that the energy liberated by this fission reaction is:  $E_{lib} = E_B (Kr) + E_B (Ba) E_B (U)$ .
- **d**) Deduce the value of  $E_{lib}$  in MeV and in joule.
- 3) We suppose that the other nuclear fission reactions, that might take place in the reactor, liberate approximately the same amount of energy as that obtained in part (2-d).
  - a) Calculate the energy liberated by the fission of 112 g of uranium 235.
  - **b**) Determine the efficiency of the reactor of the submarine knowing that it delivers an electric power of 25 MW.

### Fourth exercise: (7.5 points)

## **Photoelectric effect**

Given:  $c = 3 \times 10^8$  m/s; 1 eV =  $1.6 \times 10^{-19}$  J; h =  $6.64 \times 10^{-34}$  Js.

### **A** – Emission of photoelectrons

Let W<sub>0</sub> be the minimum energy needed to extract an electron from the surf the cathode of a photo cell and  $v_0$  the threshold frequency of this metal.

- 1) Define the threshold frequency  $v_0$ .
- 2) Write the relation between  $W_0$  and  $v_0$ .
- **3)** To determine  $W_0$  and then the nature of the metal, we illuminate the cathode of the

photo cell successively and separately each time with radiations of different frequencies and we determine the maximum kinetic energy (KE<sub>max</sub>) of the emitted photoelectrons for each radiation of frequency v. We obtain the results shown in table 1.

| Nucleus                         | $^{235}_{92}{ m U}$ | $^{91}_{36}{ m Kr}$ | <sup>A</sup> <sub>Z</sub> Ba |
|---------------------------------|---------------------|---------------------|------------------------------|
| $\frac{E_{B}}{A}$ (MeV/nucleon) | 7.59                | 8.55                | 8.31                         |

| face of a | metal | that covers | t |
|-----------|-------|-------------|---|
|           |       |             |   |

5.5

0.20

v (×10<sup>14</sup> Hz)

KE<sub>max</sub>(eV)

| Table (1) |  |
|-----------|--|
| •         |  |

6.2

0.49

6.9

0.79

7.5

1.03

**a**) Trace the curve representing the variations of  $KE_{max}$  in terms of v.

Scale: on the horizontal axis:  $1 \text{ cm} \rightarrow 10^{14} \text{ Hz}$ ; on the vertical axis:  $1 \text{ cm} \rightarrow 0.20 \text{ eV}$ .

b) i) The obtained graph confirms with Einstein's relation concerning the photoelectric effect. Justify.ii) Name the physical constant that is represented by the slope of this graph.

c) Using the graph, determine the value of:

- i) this physical constant;
- ii) the threshold frequency  $v_{0.}$
- **d**)Deduce the value of  $W_0$ .
- e) Referring to table 2, indicate the nature of the metal used.

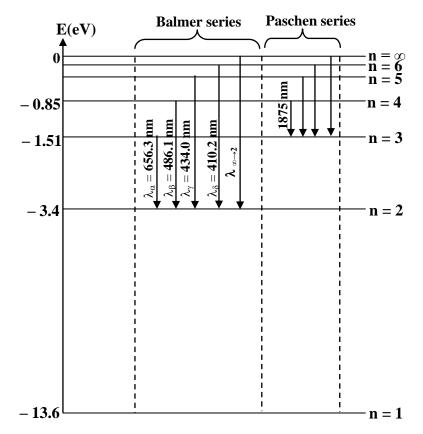
| metal      | cesium | sodium | potassium |
|------------|--------|--------|-----------|
| $W_0 (eV)$ | 2.07   | 2.28   | 2.30      |

| Table | (2) |
|-------|-----|
|-------|-----|

#### **B** – The hydrogen atom

The spectral lines that constitute the hydrogen spectrum can be classified into many series; each series corresponds to the electronic transitions that lead to the same energy level. The figure below shows two of these series with the wavelengths of some emitted radiations.

The radiations emitted by the hydrogen gas lamp illuminates the cesium cathode of a photo cell.



Consider the spectral line having the smallest wavelength of the Paschen series.
 a) To which transition does this line correspond?

**b**)Deduce the energy of the corresponding emitted photon.

c) Can the photons of the Paschen series extract photoelectrons from a cesium surface? Why?

- 2) Consider the spectral lines corresponding to the emitted radiations of wavelengths  $\lambda_{\alpha}$  and  $\lambda_{\beta}$  of Balmer series.
  - a) Referring to the above energy diagram, calculate the corresponding frequencies  $v_{\alpha}$  and  $v_{\beta}$ .
  - **b**) One of these two radiations can extract photoelectrons from the surface of cesium. Specify this radiation.

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|--------------------------------------|-------------------------------------------------------|------------------------------------------------------------------------------|--|--|
| مشروع معيار التصحيح<br>مادة الفيزياء |                                                       |                                                                              |  |  |

## First exercise: (7.5 points)

| Part of the Q | Answer                                                                                                                                                                                                                                                                                                                      | Mark |
|---------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------|
| A.1.a         | $\ell_1 = \ell + x$ and $\ell_2 = \ell - x$                                                                                                                                                                                                                                                                                 | 1/2  |
| A.1.b         | The elastic potential energy stored in the two springs is:<br>$PE_e = \frac{1}{2} k(\Delta \ell + x)^2 + \frac{1}{2} k(\Delta \ell - x)^2 = k (\Delta \ell^2 + x^2)$                                                                                                                                                        | 1    |
| A.2           | The mechanical energy of the system is:<br>$ME = \frac{1}{2} m v^2 + k (\Delta \ell^2 + x^2)$                                                                                                                                                                                                                               | 1/2  |
| A.3           | No Friction $\Rightarrow \frac{dME}{dt} = 0 \Rightarrow mvv' + 2kxx' = 0 \Rightarrow mx'' + 2kx = 0$<br>$\Rightarrow x'' + \frac{2k}{m} x = 0.$                                                                                                                                                                             | 1    |
| A.4.a         | $\begin{aligned} \mathbf{x}' &= -\omega_0 \ \mathbf{X}_m \sin(\omega_0 t + \phi) \text{ and } \mathbf{x}'' = -\omega_0^2 \mathbf{X}_m \cos(\omega_0 t + \phi). \\ \text{By replacing in the differential equation:}  \omega_0^2 &= \frac{2k}{m}. \\ \omega_0 &= \sqrt{\frac{2k}{m}} \end{aligned}$                          | 1/2  |
| A.4.b         | The value of the proper period $T_0$ is:<br>$T_0 = \frac{2\pi}{\omega_0} = 2\pi \sqrt{\frac{m}{2k}} = 2\pi \sqrt{\frac{0.51}{2 \times 10}} = 1.003 \text{ s} \approx 1 \text{ s}$                                                                                                                                           | 1/2  |
| <b>B.1.</b> a | T is slightly greater than $T_0$ because of friction.                                                                                                                                                                                                                                                                       | 1/2  |
| B.1.b         | $4 \text{ T} = 4.04 \Longrightarrow \text{T} = 1.01 \text{ s}$                                                                                                                                                                                                                                                              | 1⁄4  |
| B.2.a         | Variation of the mechanical energy:<br>$ME_0 = k (\Delta \ell^2 + x_0^2)$ at $t = 0s$<br>$ME_{4T} = k (\Delta \ell^2 + x_4^2)$ at $t = 4T$<br>$\Rightarrow \Delta ME = k[x_4^2 - x_0^2] = 10[5.57 \times 10^{-4} - 6.25 \times 10^{-4}] = -6.8 \times 10^{-4} \text{ J.}$<br>So the loss is $6.8 \times 10^{-4} \text{ J.}$ | 3⁄4  |
| B.2.b         | The lost average power: $\frac{ \Delta ME }{\Delta t} = \frac{6.8 \times 10^{-4}}{4.04} = 1.68 \times 10^{-4} \text{ W}$                                                                                                                                                                                                    | 1/2  |
| B.3.a         | Figure 5 : $X_m = 4.1$ cm and $T = \frac{4}{7} = 0.57$ s.<br>Figure 6 : $X_m = 14$ cm and $T = 1.01$ s.                                                                                                                                                                                                                     | 1    |
| B.3.b         | In the case (figure 5) we are far from the resonance $T < T_0$ and in the case (figure 6) there is a resonance $T = T_0$ .                                                                                                                                                                                                  | 1/2  |

# Second exercise: (7.5 points)

| Part of the Q | Answer                                                                                                                                                                                                 | Mark |
|---------------|--------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------|
| A.1.a         | $u_{AB} = Ri = RI\sqrt{2} sin(2\pi ft)$                                                                                                                                                                | 1/2  |
| A.1.b         | $u_{BD} = L \frac{di}{dt} + ri = 2\pi f L I \sqrt{2} \cos(2\pi f t) + rI \sqrt{2} \sin(2\pi f t)$                                                                                                      | 1/2  |
| A.2           | $u_{DM} = \frac{q}{C} \text{ but } dq = \text{idt} = I\sqrt{2} \sin(2\pi ft)dt \Rightarrow q = -\frac{I\sqrt{2}}{2\pi f}\cos(2\pi ft).$ $\Rightarrow u_{DM} = -\frac{I\sqrt{2}}{2\pi f}\cos(2\pi ft).$ | 1    |
| <b>B.1.a</b>  | $\frac{2\pi f C}{u_{AB} = u_{AB} + u_{BD} + u_{DM}}$                                                                                                                                                   | 2    |
| <b>D</b> .1.a | $U\sqrt{2} \sin(2\pi ft + \varphi) = (2\pi fL - \frac{1}{2\pi fC})I\sqrt{2}\cos(2\pi ft) + (R + r)I\sqrt{2}\sin(2\pi ft)$                                                                              | 2    |
|               | For $2\pi ft = 0$ we get: Usin $\phi = I \left(2\pi f_0 L - \frac{1}{2\pi f C}\right)$ (1)                                                                                                             |      |
|               | For $2\pi ft = \frac{\pi}{2}$ we get: Ucos $\varphi = I(R+r)$ (2)                                                                                                                                      |      |
|               | Squaring and adding (1) and (2), we get:                                                                                                                                                               |      |
|               | $U^{2} = \left[ (R+r)^{2} + (2\pi f L - \frac{1}{2\pi f C})^{2} \right] I^{2}$ U                                                                                                                       |      |
|               | $\Rightarrow I = \frac{U}{\sqrt{(R+r)^2 + (2\pi f L - \frac{1}{2\pi f C})^2}} .$                                                                                                                       |      |
| B.1.b         | The ratio $\frac{(1)}{(2)}$ ) gives: $\tan \varphi = \frac{2\pi f L - \frac{1}{2\pi f C}}{R+r}$ .                                                                                                      | 1/2  |
| <b>B.2.a</b>  | Current resonance                                                                                                                                                                                      | 1⁄4  |
| B.2.b         | $I = I_0 = 160 \text{ mA.}$                                                                                                                                                                            | 1/2  |
| B.2.c.i       | According to the relation (B-1-b), i and $u_{AM}$ are in phase                                                                                                                                         | 3⁄4  |
|               | $\Rightarrow \phi = 0 \Rightarrow \tan \phi = 0 \Rightarrow 2\pi f_0 L - \frac{1}{2\pi f_0 C} = 0 \Rightarrow 4\pi^2 f_0^2 LC = 1$                                                                     |      |
| B.2.c.ii      | The relation (B-1-a) becomes $U = (R + r)I \Rightarrow$ the circuit is equivalent to a resistor of resistance $R_t = R + r$ .                                                                          | 1/2  |
| B.2.d         | The relation $4\pi^2 f_0^2 LC = 1 \implies L = 0.1 H$                                                                                                                                                  | 1/2  |
| <b>B.2.</b> e | At resonance the expression $U = (R + r)I \Rightarrow (R + r) = 50 \Rightarrow r = 20 \Omega$                                                                                                          | 1/2  |

## Third exercise: (7.5 points)

| Part of<br>the Q | Answer                                                                                                                                                                  | Mark |
|------------------|-------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------|
| 1.a              | Conservation of mass number: $1 + 235 = 91 + Y + 3 \Rightarrow Y = 142$                                                                                                 | 1    |
|                  | Conservation of charge number: $0 + 92 = 36 + X + 0 \Longrightarrow X = 56$                                                                                             | •    |
| 1.b              | The nuclear reaction is provoked, because it needs an external                                                                                                          | 1/2  |
|                  | intervention : bombarded with a thermal neutron                                                                                                                         |      |
| 1.c              | The neutron must be thermal (low kinetic energy)                                                                                                                        | 1/2  |
| 2.a              | Since $E_B(X) = A \frac{E_{B(X)}}{A}$ , then:                                                                                                                           | 1    |
|                  | $E_B(U) = 235 \times 7.59 = 1783.65 \text{ MeV};$                                                                                                                       |      |
|                  | $E_{\rm B}$ (Kr) = 91×8.55 = 778.05 MeV;                                                                                                                                |      |
|                  | $E_B$ (Ba) = 142×8.31 = 1180.02 MeV.                                                                                                                                    |      |
| 2.b              | $E_{B(X)} = [Z \times m_P + (A - Z)m_n - m_X]c^2$                                                                                                                       | 1/2  |
| 2.c              | $m_{X} = [Z \times m_{P} + (A - Z)m_{n}] - \frac{E_{B(X)}}{c^{2}}$                                                                                                      | 11/2 |
|                  | $E_{lib} = \left\{ \left[ m_n + (92 \ m_P + (235 - 92)m_n - \frac{E_{B(U)}}{c^2} \right] \right\}$                                                                      |      |
|                  | $-[(36 m_{\rm P} + (91 - 36)m_{\rm n} - \frac{E_{\rm B(Kr)}}{c^2})]$                                                                                                    |      |
|                  | $-\left[(56 \text{ m}_{\text{P}} + (142 - 56) \text{m}_{\text{n}} - \frac{\text{E}_{\text{B(Ba)}}}{\text{c}^{2}}\right)\right]$                                         |      |
|                  | $-(3m_n)$ $c^2$                                                                                                                                                         |      |
| 2.1              | $E_{lib} = E_B (Kr) + E_B (Ba) - E_B (U)$                                                                                                                               |      |
| 2.d              | $\begin{split} E_{lib} &= 1180.02 + 778.05 - 1783.65 = 174.42 \text{ MeV}.\\ E_{lib} &= 174.42 \times 1.6 \times 10^{-13} = 2.79 \times 10^{-11} \text{ J} \end{split}$ | 3⁄4  |
| <b>3.</b> a      | 1 fission reaction $\rightarrow 3.9 \times 10^{-25} \text{ kg} \rightarrow 2.79 \times 10^{-11} \text{ J}$<br>0.112 kg $\rightarrow ?$                                  | 3⁄4  |
|                  | The energy liberated by the fission of 112 g is: $8.0123 \times 10^{12}$ J.                                                                                             |      |
| <b>3.</b> b      | $P = \frac{E}{t} = \frac{8.0123 \times 10^{12}}{24 \times 3600} = 9.2735 \times 10^7 \text{ watt}$                                                                      | 1    |
|                  | The efficiency of the reactor is : $\xi = \frac{25 \times 10^6}{92.735 \times 10^6} = 0.269 = 26.9\%$                                                                   |      |

| Part of the Q | Answer                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        | Mark |
|---------------|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------|
| A.1           | The threshold frequency $v_0$ of a metal is the minimum frequency of an electromagnetic wave that can extract an electron when it illuminates the metal.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | 1/2  |
| A.2           | $\mathbf{W}_0 = \mathbf{h} \ \mathbf{v}_0.$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   | 1⁄4  |
| A.3.a         | $\begin{array}{c} & & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & & \\ & &$ | 11/2 |
| A.3.b.i       | $h\nu = W_0 + KE_{max} \Rightarrow KE_{max} = h\nu - h\nu_0$ which is a linear function of the                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | 1/2  |
| A.3.b.ii      | frequency v.<br>The slope of the graph is h (Planck's constant)                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 1/   |
| A.3.c.i       |                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               | 1/4  |
| A.J.C.I       | $h = \frac{\Delta KE_{max}}{\Delta v} \Longrightarrow h = \frac{(1.03 - 0.2) \times 1.6 \times 10^{-19}}{(7.5 - 5.5) \times 10^{14}} = 6.64 \times 10^{-34} \text{ Js}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       | 1    |
| A.3.c.ii      | $v_0 = 5 \times 10^{14} \text{ Hz},$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 1⁄4  |
| A.3.d         | $W_0 = hv_0 = 6.64 \times 10^{-34} \times 5 \times 10^{14} = 3.32 \times 10^{-19} \text{ J};$<br>$W_0 = \frac{3.32 \times 10^{-19}}{1.6 \times 10^{-19}} = 2.075 \text{ eV}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  | 1/2  |
| A.3.e         | The used metal is cesium.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     | 1⁄4  |
| <b>B.1.a</b>  | The smallest wavelength in the Paschen series corresponds to the transition from $n = \infty$ to $n = 3$ .                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    | 1⁄2  |
| <b>B.1.</b> b | The energy of the corresponding photon is: $E_{\infty} - E_3 = 1.51$ eV.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      | 1/2  |
| <b>B.1.</b> c | No, because the maximum of energy of the emitted photon in Paschen series is 1.51 eV which is less than 2.075 eV                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              | 1/2  |
| B.2.a         | We know that $v = \frac{c}{\lambda}$<br>$\Rightarrow v_{\alpha} = \frac{3 \times 10^8}{656.3 \times 10^{-9}} = 4.57 \times 10^{14} \text{ Hz.};$<br>$v_{\beta} = \frac{3 \times 10^8}{486.10 \times 10^{-9}} = 6.17 \times 10^{14} \text{ Hz}$                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                | 1/2  |
| B.2.b         | The radiation of frequency $\nu_{\alpha} < \nu_0$ does not emit photoelectrons;<br>while $\nu_{\beta} > \nu_0$ emits photoelectrons.                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          | 1⁄2  |

# Fourth exercise (7.5 points)